

# PROPERTIES OF SHAPES

## Key Concepts

### Lines of symmetry

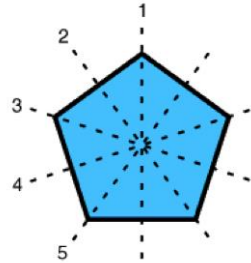
The number of lines that cut an image in half such that each half of the figure is the mirror image of the other half.

### Order of rotation

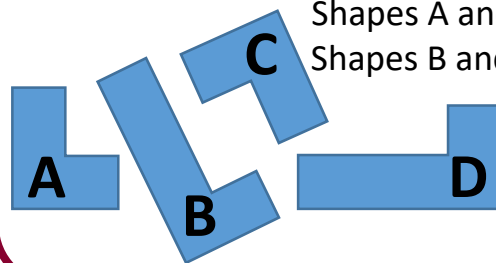
The number of times a figure fits into itself in one complete rotation of 360 degrees.

### Congruent shapes

Images that are identical to one another. They can be flipped or rotated, not enlarged.



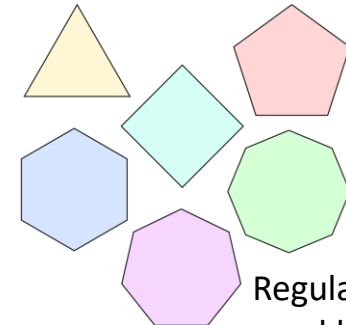
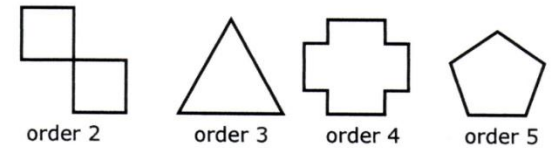
This regular polygon has 5 lines of symmetry



Shapes A and C are congruent.  
Shapes B and D are congruent.

## Examples

### Order of rotation



Regular shapes have equal lengths of sides and equal angles.

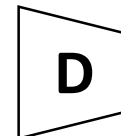
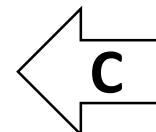
**sparx**

M276, M618,  
M276, M523

## Key Words

Rotation  
Symmetry  
Congruent  
Regular  
Irregular

- 1) How many lines of symmetry does shape B have?
- 2) What is the order of rotation of shape E?
- 3) Which shape is congruent to shape A?
- 4) Which shape is regular?



## Questions

# TYPES OF ANGLE AND ANGLES IN POLYGONS

## Key Concepts

**Regular polygons** have equal lengths of sides and equal angles.

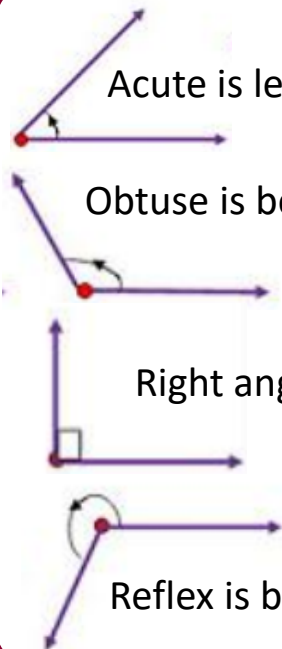
### Angles in polygons

Sum of interior angles  
 $= (\text{number of sides} - 2) \times 180$

Exterior angles of **regular** polygons  
 $= \frac{360}{\text{number of sides}}$

### Types of angle

There are four types which need to be identified – acute, obtuse, reflex and right angled.



Acute is less than  $90^\circ$

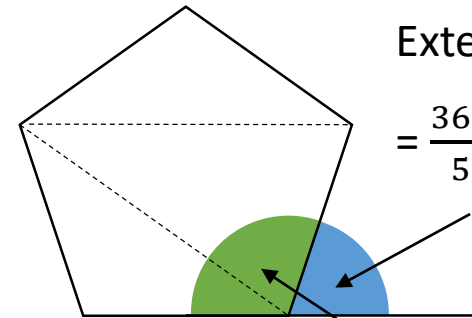
Obtuse is between  $90^\circ$  and  $180^\circ$

Right angled is  $90^\circ$

Reflex is between  $180^\circ$  and  $360^\circ$

## Examples

Regular Pentagon



Exterior angles

$$= \frac{360}{5} = 72^\circ$$

Sum of interior angles  
 $= (5 - 2) \times 180$   
 $= 540^\circ$

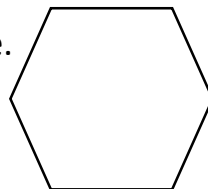
$$\text{Interior angle} = \frac{540}{5} = 108^\circ$$

## Key Words

Polygon  
 Interior angle  
 Exterior angle  
 Acute  
 Obtuse  
 Right angle  
 Reflex

## Questions

- 1) Calculate the sum of the interior angles for this regular shape.
- 2) Calculate the exterior angle for this regular shape.
- 3) Calculate the size of one interior angle in this regular shape.



**sparx**

M502

M679

M653

# ANGLE FACTS INCLUDING ON PARALLEL LINES

## Key Concepts

Angles in a **triangle equal 180°**.

Angles in a **quadrilateral equal 360°**.

**Vertically opposite angles** are equal in size.

Angles on a **straight line equal 180°**.

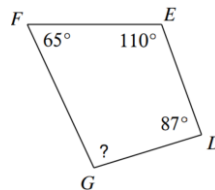
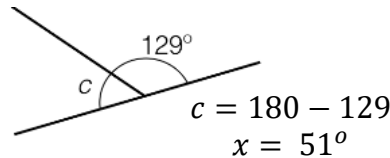
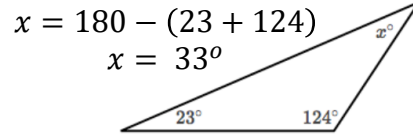
**Base angles in an isosceles triangle** are equal.

**Alternate angles** are equal in size.

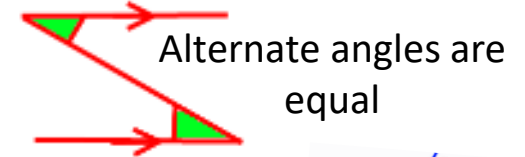
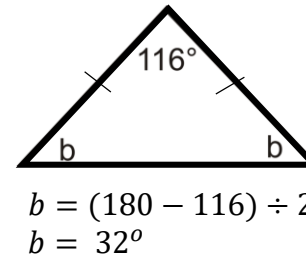
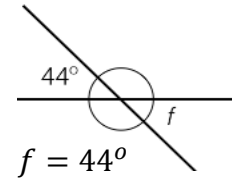
**Corresponding angles** are equal in size.

**Allied/co-interior angles** are equal 180°.

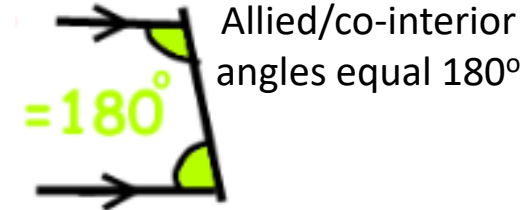
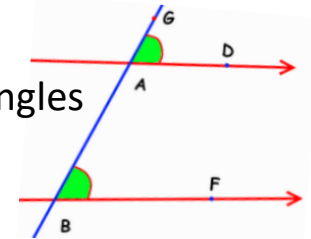
## Examples



$? = 360 - (65 + 110 + 87)$   
 $? = 98^\circ$



Corresponding angles are equal



**sparx**

**M331**

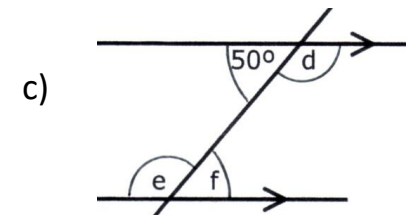
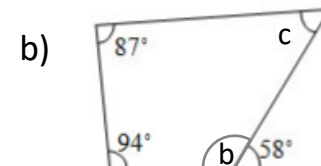
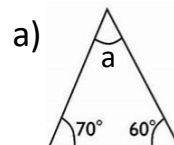
**M606**

## Key Words

Angle  
Vertically opposite  
Straight line  
Alternate  
Corresponding  
Allied  
Co-interior

## Questions

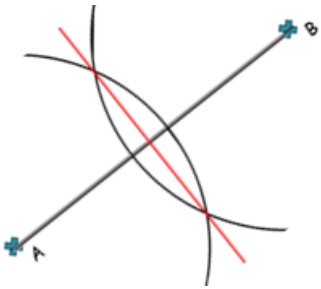
Calculate the missing angle:



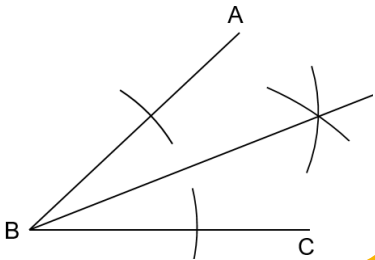
# CONSTRUCTIONS

## Key Concept

Line Bisector



Angle Bisector



## Key Words

**Construction:** To draw a shape, line or angle accurately using a compass and ruler.

**Loci:** Set of points with the same rule.

**Parallel:** Two lines which never intersect.

**Perpendicular:** Two lines that intersect at  $90^\circ$ .

**Bisect:** Divide into two parts.

**Equidistant:** Equal distance.

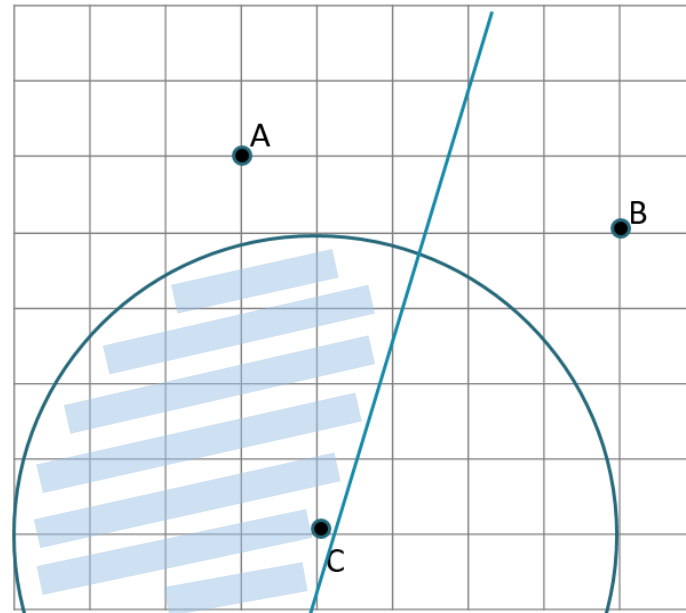
## Examples

Shade the region that is:

- closer to A than B
- less than 4 cm from C

Line bisector of A and B

Circle with radius 4cm



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M253,U820

## Tip

Watch for scales.

For a scale of:

1 cm = 4 km.

20 km = 5 cm

6 cm = 24 km

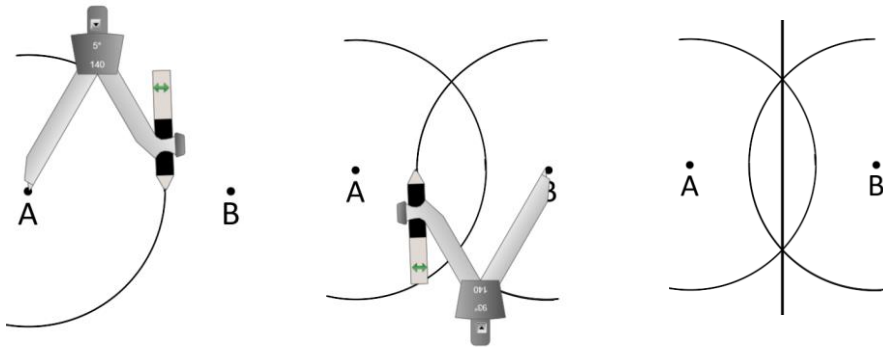
## Questions

- 1) Draw these angles then bisect them using constructions:  
a)  $46^\circ$     b)  $18^\circ$     c)  $124^\circ$
- 2) Draw these lines and bisect them:    a) 6cm    b) 12cm

# CONSTRUCTIONS

## Examples

### Bisect the distance between two points.

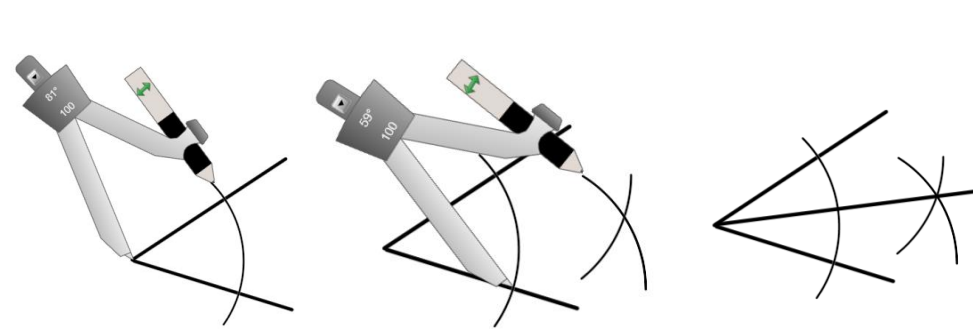


1) Open your compasses past halfway between the two points and draw an arc.

2) Keep your compasses at the same width and repeat from the other point.

3) Draw a line joining the two points where the arcs cross

### Bisect an angle.



1) Open your compasses and draw an arc over both lines from the angle

2) Keep your compasses at the same width and draw two further arcs with the point of your compasses at the intersections.

3) Draw a line joining the two points where the arcs cross and the angle point

**sparx**

M239  
M232

### Key Words

Compass  
Bisect  
Angle  
Arc

Try and recreate the above two constructions on paper using a pair of compasses and a pencil and ruler.

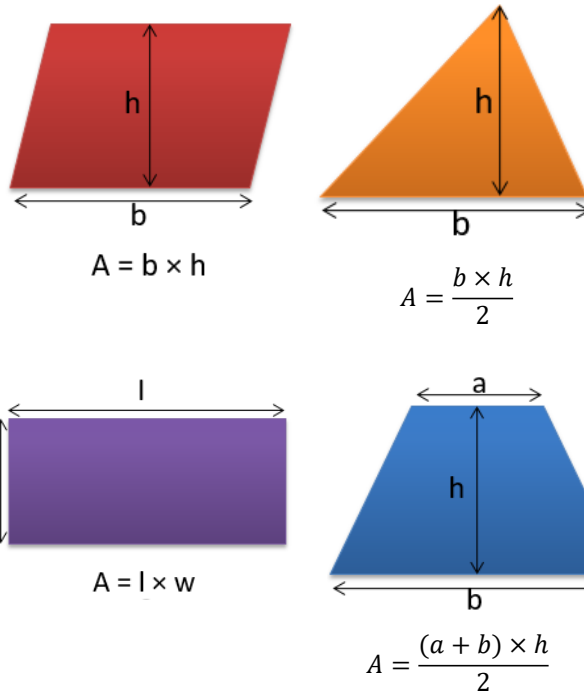
# AREA AND PERIMETER OF BASIC SHAPES

## Key Concepts

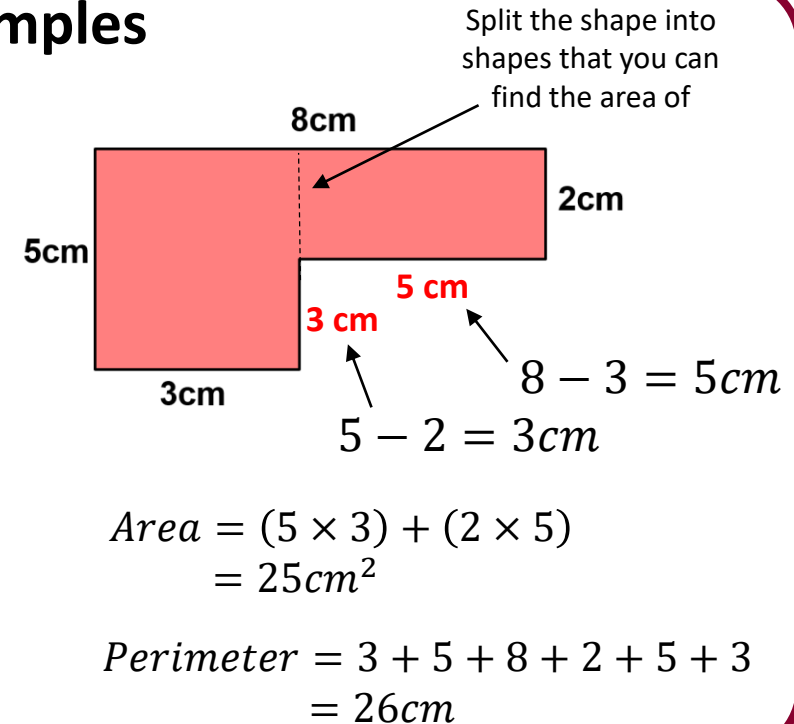
The **area** of a 2D shape is the space inside it. It is measured in units squared e.g.  $\text{cm}^2$

The **perimeter** of a shape is the distance around the edge of the shape. Units of length are used to measure perimeter e.g. mm, cm, m

A **compound shape** is a shape made up of others joined together.



## Examples



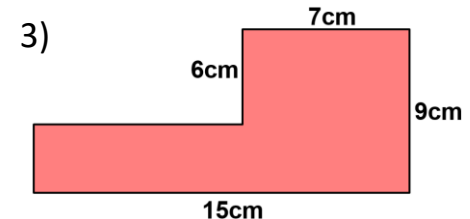
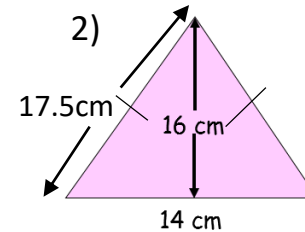
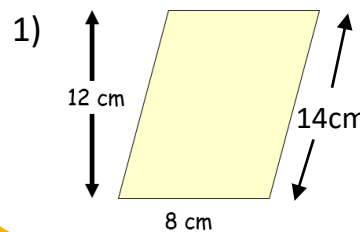
**sparx**

M635, M690, M900,  
M269, M390, M635,  
M610, M996

## Key words

Area  
Perimeter  
Base  
Height  
Width  
Length

Calculate the area and perimeter of each shape:

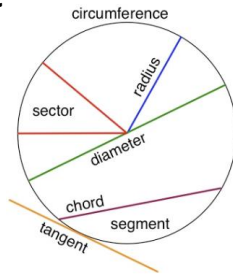


ANSWERS: 1)  $A = 96\text{cm}^2$   $P = 44\text{cm}$  2)  $A = 112\text{cm}^2$   $P = 49\text{cm}$  3)  $A = 87\text{cm}^2$   $P = 48\text{cm}$

# PERIMETER AND CIRCUMFERENCE

## Key Concepts

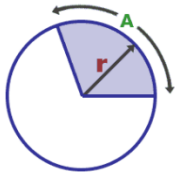
### Parts of a circle



### Circumference

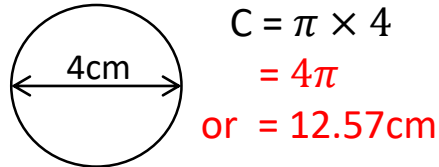
of a circle is calculated by  $\pi d$  and is the distance around the circle.

**Arc length** of a sector is calculated by  $\frac{\theta}{360} \pi d$ .



Calculate:

### a) Circumference



$$C = \pi \times 4$$

$$= 4\pi$$

$$\text{or } = 12.57\text{cm}$$

### b) Diameter when the circumference is 20cm

$$C = \pi \times d$$

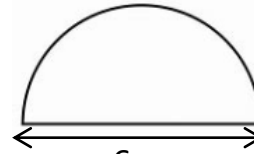
$$20 = \pi \times d$$

$$\frac{20}{\pi} = d$$

$$\text{Or } 6.37\text{cm}$$

## Examples

### c) Perimeter



$$P = \frac{\pi \times d}{2} + d$$

$$P = \frac{\pi \times 6}{2} + 6$$

$$P = 3\pi + 6$$

$$\text{Or } = 15.42\text{cm}$$

### d) Arc length

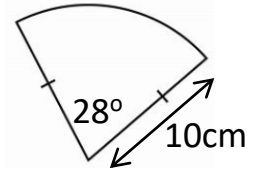
$$\text{Arc} = \frac{\theta}{360} \times \pi \times d$$

$$\text{Arc} = \frac{28}{360} \times \pi \times 2 \times 10$$

$$\text{Arc} = \frac{28}{360} \times \pi \times 20$$

$$\text{Arc} = \frac{14}{9} \pi$$

$$\text{Or } = 4.89\text{cm}$$

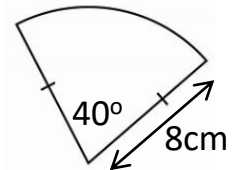


### Key Words

Circle  
Perimeter  
Circumference  
Radius  
Diameter  
Pi  
Arc

Calculate:

- 1) The circumference of a circle with a diameter of 12cm
- 2) The diameter of a circle with a circumference of 30cm
- 3) The perimeter of a semicircle with diameter 15cm
- 4) The arc length of the diagram



sparx

U604 U950 U221

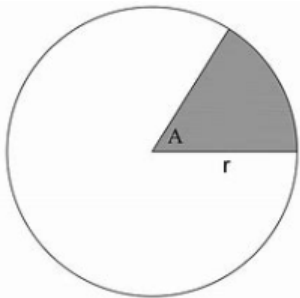
ANSWERS: 1)  $12\pi$  or 37.7cm 2)  $\frac{\pi}{30}$  or 9.54cm 3) 38.56cm 4)  $\frac{6}{16}\pi$  or 5.59cm

# AREA OF CIRCLES AND PART CIRCLES

## Key Concepts

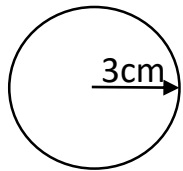
The **area** of a circle is calculated by  $\pi r^2$

The **area of a sector** is calculated by  $\frac{\theta}{360} \pi r^2$



Calculate:

a) **Area**



$$A = \pi \times 3^2$$

$$= 9\pi$$

$$\text{or} = 28.3\text{cm}^2$$

b) **Radius** when the area is  $20\text{cm}^2$

$$A = \pi \times r^2$$

$$20 = \pi \times r^2$$

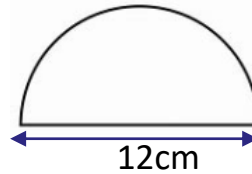
$$\frac{20}{\pi} = r^2$$

$$\sqrt{\frac{20}{\pi}} = r$$

$$\text{Or } 2.52\text{cm}$$

## Examples

c) **Area**



$$P = \frac{\pi \times r^2}{2}$$

$$P = \frac{\pi \times 6^2}{2}$$

$$P = 18\pi$$

$$\text{Or} = 56.55\text{cm}^2$$

d) **Area of a sector**

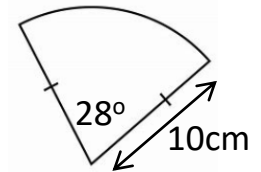
$$\text{Arc} = \frac{\theta}{360} \times \pi \times r^2$$

$$\text{Arc} = \frac{28}{360} \times \pi \times 10^2$$

$$\text{Arc} = \frac{28}{360} \times \pi \times 100$$

$$\text{Arc} = \frac{70}{9} \pi$$

$$\text{Or} = 24.43\text{cm}$$



**sparx**

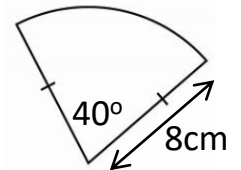
U604 U950  
U221 U373

## Key Words

Circle  
Area  
Radius  
Diameter  
Pi  
Sector

Calculate:

- 1) The area of a circle with a radius of 9cm
- 2) The radius of a circle with an area of  $45\text{cm}^2$
- 3) The area of a semicircle with diameter of 16cm
- 4) The area of the sector in the diagram



ANSWERS: 1)  $81\pi$  or  $254.47\text{cm}^2$  2)  $\sqrt{\frac{45}{\pi}}$  or  $3.78\text{cm}$  3)  $32\pi$  or  $100.53\text{cm}^2$  4)  $\frac{9}{64}\pi$  or  $22.34\text{cm}^2$



# REFLECTION, ROTATION AND TRANSLATION

## Key Concepts

A **reflection** creates a mirror image of a shape on a coordinate graph. The mirror line is given by an equation eg.  $y = 2$ ,  $x = 2$ ,  $y = x$ . The shape does not change in size.

A **rotation** turns a shape on a coordinate grid from a given point. The shape does not change size but does change orientation.

A **translation** moves a shape on a coordinate grid. Vectors are used to instruct the movement:

$\begin{pmatrix} x \\ y \end{pmatrix}$  → Positive-Right  
           → Negative - Left  
 $\begin{pmatrix} x \\ y \end{pmatrix}$  → Positive-Up  
           → Negative - Down

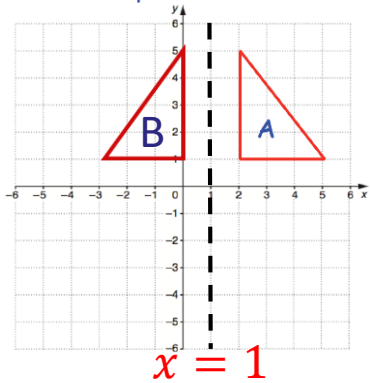
A **reflection** creates a mirror image of a shape on a coordinate graph. The mirror line is given by an equation eg.  $y = 2$ ,  $x = 2$ ,  $y = x$ . The shape does not change in size.

U134, U196,  
U696, U799

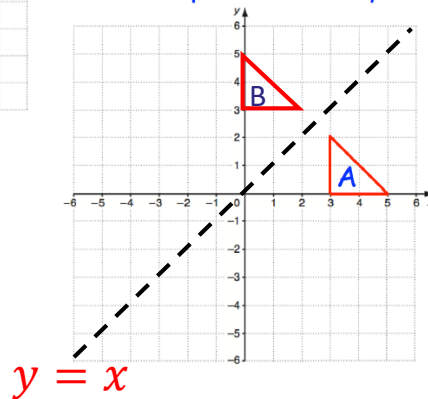
## Key Words

Rotate  
 Clockwise  
 Anticlockwise  
 Centre  
 Degrees  
 Reflect  
 Mirror image  
 Translate  
 Vector

Reflect shape A in the line  $x = 1$ . Label it B.

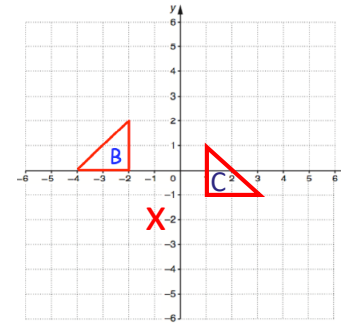


Reflect shape A in the line  $y = x$ . Label it B.

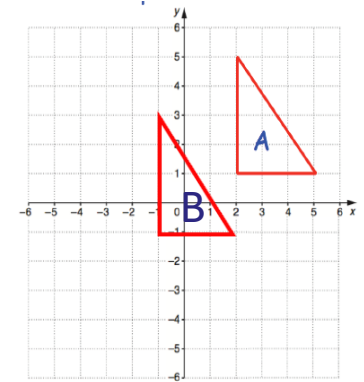


## Examples

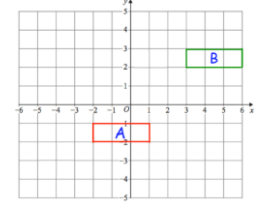
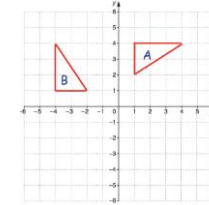
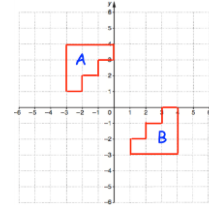
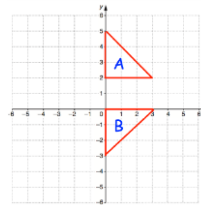
Rotate shape B from the point  $(-1, -2)$



Translate shape A by  $\begin{pmatrix} -3 \\ -2 \end{pmatrix}$ . Label it B.



Describe the **single** transformation you see on each coordinate grid from A to B:



ANSWERS: a) reflection,  $y = 1$  b) reflection  $y = x$  c) rotation, centre  $(0,0)$ ,  $90^\circ$  anticlockwise d) translation  $\begin{pmatrix} 4 \\ 5 \end{pmatrix}$