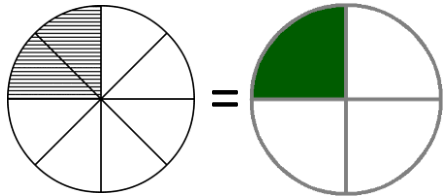


RATIO AND SCALE

Key Concept

$$2 \text{ parts} \rightarrow 2:6 \leftarrow 6 \text{ parts}$$

$$= 1:3$$



$$= \frac{1}{3}$$

Key Words

Ratio: Relationship between two numbers.

Part: This is the numeric value '1' of, would be equivalent to.

Simplify: Divide both parts of a ratio by the same number.

Equivalent: Equal in value.

Convert: Change from one form to another.

Examples

Simplify 60 : 40 : 100

$$\div 10$$

$$6 : 4 : 10$$

$$\div 2$$

$$3 : 2 : 5$$

This could have been done in one step by dividing by 20.

Write 2 : 5 in the form 1 : n

$$\begin{array}{ccc} & 2 : 5 & \\ \div 2 \swarrow & & \searrow \div 2 \\ & 1 : 2.5 & \end{array}$$

Share £45 in the ratio 2 : 7

$$2 : 7$$

5	5
5	5

$$=10$$

5
5
5
5
5

$$=35$$

$$45 \div 9 = 5$$

$$\pounds 10 : \pounds 35$$

Joy and Martin share money in the ratio 2 : 5. Martin gets £18 more than Joy. How much do they each get?

$$2 : 5$$

6	6
6	6

6
6
6
6

$$18 \div 3 = 6$$

$$\pounds 12 : \pounds 30$$

$$=12 \quad =30$$

sparx

M981,U171,
U680

Tip

Its often useful to write the letters above the ratio. This helps you keep the order the correct way round.

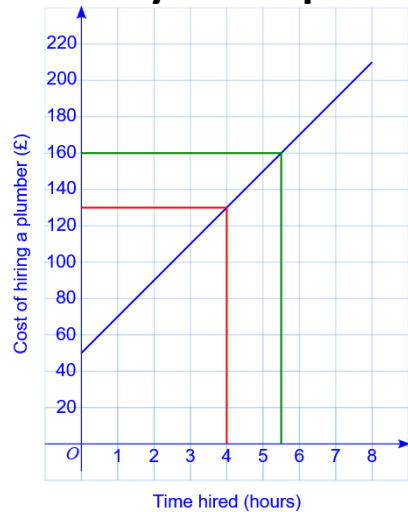
Questions

- 1) Simplify a) 45 : 63 b) 66 : 44 c) 320 : 440
- 2) Write in the form 1 : n a) 5 : 10 b) 4 : 6 c) $x : x^2 + x$
- 3) Share 64 in the ratio 3 : 5 4) Write the ratio 1 : 4 as a fraction.

ANSWERS: 1) a) 5 : 7 b) 3 : 2 c) 8 : 11 2) a) 1 : 2 b) 1 : 1.5 c) $1 : x + 1$ 3) 24 : 40 4) $\frac{1}{5}$

MULTIPLICATIVE CHANGE

Key Concept



Gradient – The extra cost incurred for every extra hour.
y-intercept – The minimum payment to the plumber.

Key Words

Conversion graph: A graph which converts between two variables.

Intercept: Where two graphs cross.

y-intercept: Where a graph crosses the y-axis.

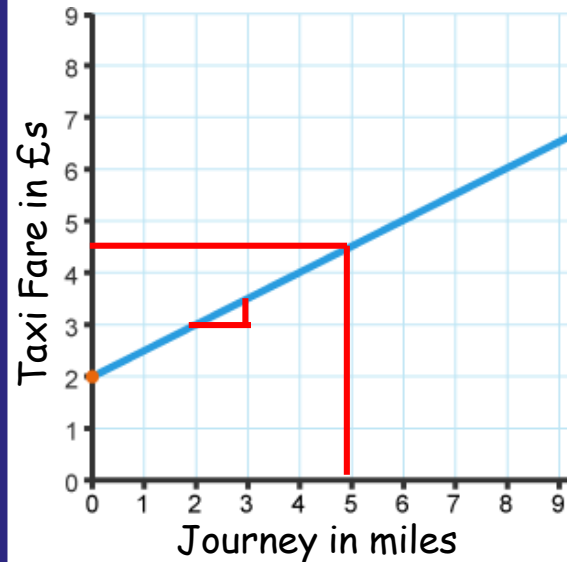
Gradient: The rate of change of one variable with respect to another. This can be seen by the steepness.

Simultaneous: At the same time.

Tip

The solution to two linear equations with two unknowns is the coordinates of the intercept (where they cross).

Examples



What is the minimum taxi fair?
£2, this is the y-intercept.

What is the charge per mile?
50p, every extra mile adds on 50p.

How much would a journey of 5 miles cost?
£4.50, See line drawn up from 5 miles to the graph, then drawn across to find the cost.

sparx

**M932, M658
M843, M771**

Questions

- 1) For the graph above
 - a) A journey is 8 miles, what is its cost?
 - b) A journey cost just £3, how far was the journey?
- 2) Draw a graph to show the exchange rate $\text{£}1 = \text{\$}1.4$.

OPERATIONS WITH FRACTIONS

Key Concept

Mixed numbers

These are made up of a whole number and a fraction.





$$4\frac{3}{5}$$

$$= \frac{4 \times 5 + 3}{5}$$

$$= \frac{23}{5}$$

Key Words

Fraction: A fraction is made up of a numerator (top) and a denominator (bottom).

 <p>Add Sum Total All together Plus In all</p>	 <p>Multiply Product Times Twice Total Multiplied by</p>
 <p>Subtract Remain Difference Less than Fewer How many more Minus</p>	 <p>Divide Quotient Goes into Split Equally Each</p>

Tip

- A larger denominator **does not** mean a larger fraction.
- To find equivalent fractions multiply/divide the numerator and denominator by the same number.

Examples

$$+ \quad \frac{3}{5} + \frac{2}{7}$$

Make the denominators the same

$$\frac{3}{5} + \frac{2}{7}$$

$\times 7$ $\times 5$

$$\frac{21}{35} + \frac{10}{35} = \frac{31}{35}$$

$$- \quad \frac{3}{5} - \frac{2}{7}$$

$$\frac{3}{5} - \frac{2}{7}$$

$\times 7$ $\times 5$

$$\frac{21}{35} - \frac{10}{35} = \frac{11}{35}$$

4 Rules
Fractions

$$\times \quad \frac{3}{5} \times \frac{2}{7}$$

Just multiply the tops and bottoms

$$= \frac{3 \times 2}{5 \times 7} = \frac{6}{35}$$

$$\div \quad \frac{3}{5} \div \frac{2}{7}$$

Flip the second fraction and change to a times

$$\frac{3}{5} \times \frac{7}{2} = \frac{21}{10}$$

sparx

M671, M939, M601,
M835, M931, M157,
M197, M110

Questions

1) $\frac{3}{5} + \frac{4}{15}$ 2) $\frac{2}{7} + \frac{5}{8}$ 3) $\frac{7}{9} - \frac{2}{5}$ 4) $\frac{3}{7} \times \frac{4}{9}$ 5) $\frac{3}{11} \div \frac{14}{22}$

ANSWERS: 1) $\frac{13}{15}$ 2) $\frac{51}{56}$ 3) $\frac{17}{45}$ 4) $\frac{21}{4}$ 5) $\frac{7}{3}$

NUMBER SENSE

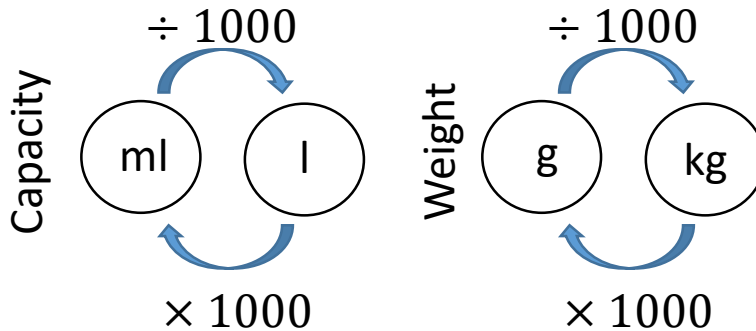
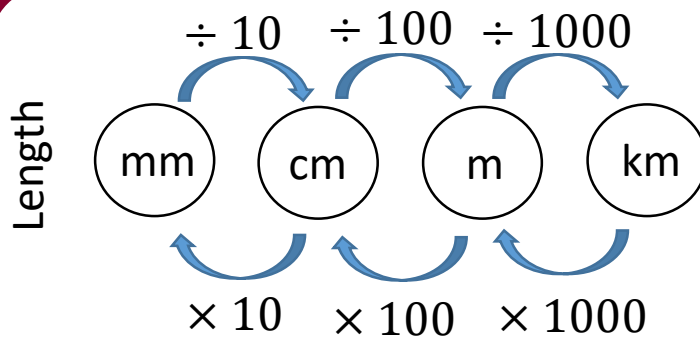
Key Concept

Metric units of **length**:
mm, cm, m, km

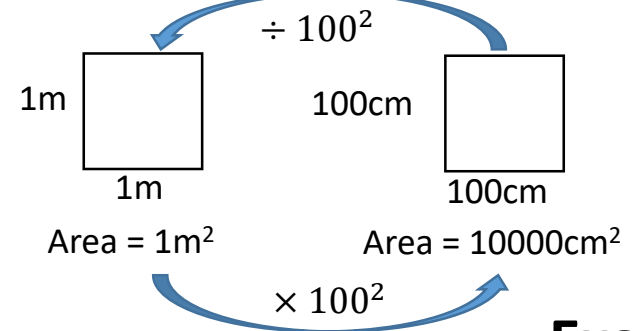
Metric units of **weight**:
g, kg

Metric units of **capacity**:
ml, l

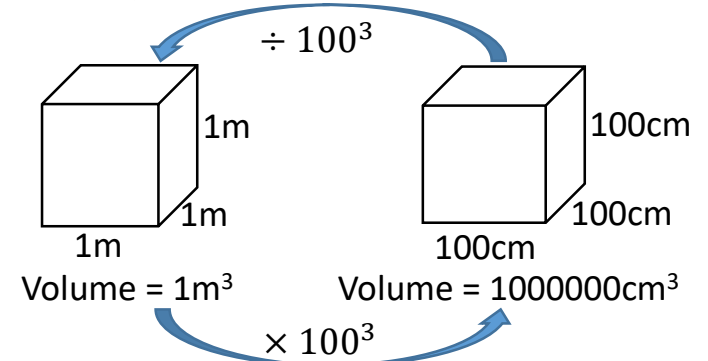
All of these units are **metric** units. They will always use conversions of multiples of 10, eg. 10, 100, 1000 etc.



Converting areas



Converting volumes



Examples

sparx
M487

Key Words

Length
Weight
Capacity
Metric

Convert each of the following:

- a) 12cm into mm
- b) 1783g into kg
- c) 2.5 litres into ml
- d) 6.8m into mm
- e) 5000000cm^3 into m^3
- f) 2m^2 into cm^2